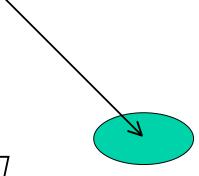
#### Irradiance

- Irradiance is the amount of light (power) falling on a surface per unit area.
- Units are watts/m<sup>2</sup>
- Generally a function of direction

$$E(\underline{x}, [], []) = \frac{[P(\underline{x})]}{[A]} = L(\underline{x}, [], []) \quad [] \quad \cos[]$$



#### Irradiance

- Note that irradiance is the incident power per unit area *not foreshortened*.
- A surface experiencing radiance L(x,□,□) coming from d□ experiences irradiance

$$L(\underline{x}, \square, \square) \cos \square d\square$$

- Total power arriving at the surface is given by adding irradiance over all incoming angles.
- Total power is:

For integration in polar coords

### BRDF (Bidirectional reflectance distribution function)

The irradiance at a point due to a particular angle is

$$L_i(\underline{x}, \underline{\square}_i, \underline{\square}_i) \cos \underline{\square}_i d\underline{\square}$$

• The energy leaving (reflected) in a particular outgoing direction is given by:

$$L_o(\underline{x},\underline{\square}_o,\underline{\square}_o)$$

• The BRDF is simply the ratio of the output to input.

$$\prod_{bd} \left( \underline{x}, \prod_{o}, \prod_{o}, \prod_{i}, \prod_{i} \right) = \frac{L_{o}(\underline{x}, \prod_{o}, \prod_{o})}{L_{i}(\underline{x}, \prod_{i}, \prod_{i}) \cos \prod_{i} d \prod_{o}}$$

- Units are inverse steradians (sr-1)
- Symmetric in incoming and outgoing directions
  - Has been argued based on thermodynamics (some debate on the validity of such arguments), but regardles, it is not simply a function of the formulation---it depends on fundemental assumptions regarding the nature of the world.
- Note that the form of the BRDF, while a bit odd looking due to the assymetry of the numerator versus denominator, makes sense. If you attempt to measure light out relativel to light in, the light out is a function of the size of the sample and its angle, both which are not intrisic surface properties.
- Thus the BRDF has to normalize for these quantities

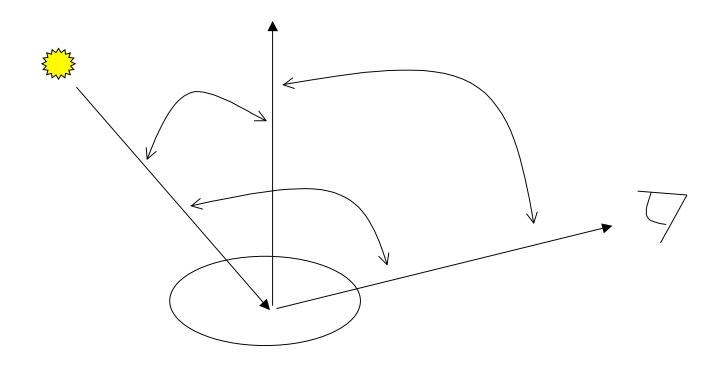
- The "distribution" part of the name is a hint that we need to integrate the function to get some light.
- To compute the brightness of a surface viewed from a given direction, we add up the contributions from all the input directions:

- Note that what we have developed so far is mostly notation, definitions, and descriptions.
- Two approaches to obtaining BRDF's--measure and model.
- Measuring BRDF is painful (but there is some data available on-line (and more clever ways to collect the have been proposed).
- Developing physics based approximations for the BRDF for simple classes of surfaces is complicated but possible--this is still an active research area.
- Adding color to the BRDF is easy (one more variable). The full form has additional variables for fluorescence and polarization.

- So why do we care about the BRDF?
  - If you have it, then you can compute the effect of any illumination distribution--a photograph only tells you the effect of one illumination distribution
  - Useful abstraction--surface reflection can be quite complex!

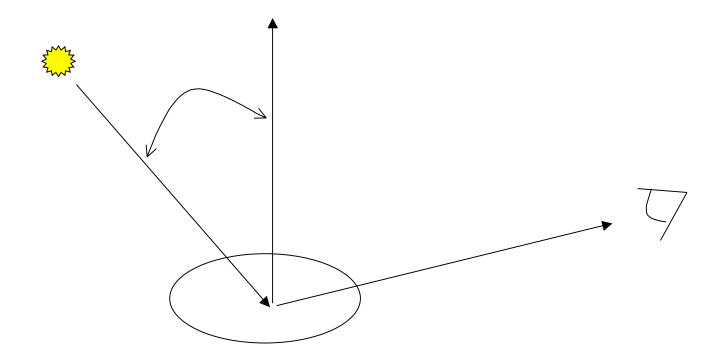
## Isotropic surfaces

The BRDF for many surfaces can be well approximated as a function of 3 variables (angles), not 4. In this case, turning the surface around the normal has no effect. The surface is said to be *isotropic*.



#### Lambertian surfaces

• Even simpler case--the BRDF does not depend on the viewing (output) direction (e.g., Lambertian).



#### Lambertian surfaces and albedo

- For some surfaces, the percentage of arriving light that leaves is independent of direction in which it arrived
- Lambertian surfaces / ideal diffuse surfaces
  - cotton cloth, carpets, matte
     paper, matte paints, etc.

- Use radiosity as a unit to describe light leaving the surface (def'n next slide)
- Percentage of light leaving the surface is often called diffuse reflectance, or *albedo* for a Lambertian surface.

## Radiosity

- Again, in many situations, we do not need angle coordinates at all
  - e.g. cotton cloth, where the reflected light is not dependent on angle
- Radiometric unit is radiosity
  - total power leaving a point on the surface, per unit area on the surface (Wm<sup>-2</sup>)

- Radiosity from radiance?
  - sum radiance leaving surface over all exit directions

$$B(\underline{x}) = \prod_{o} (\underline{x}, [], []) \cos[]d[]$$
Optional

#### Sources and Exitance

- Exitance of a source is
  - the internally generated power radiated per unit area on the radiating surface
- A source will have both
  - radiosity, because it reflects
  - exitance, because it emits

Radiosity leaving = Exitance + Radiosity due to incoming light

# Standard nearby point source model (Lambertian reflection)

$$\square_{d}(x) = N(x) \cdot S(x)$$

$$\Gamma(x)^{2} = \Gamma(x)^{2}$$

- N is the illuminated surface normal
- rho is diffuse albedo
- S is source vector a vector from x to the source, whose length is the intensity term
  - works because a dot-product is basically a cosine
- r(x) is distance from surface point to source --- term occurs because source "looks smaller" as we move away--or, alternatively, its energy is spread out over a larger surface.

## Standard distant point source model

- Nearby point source gets bigger if one gets closer, but the effect for far away points is negligible (e.g. the sun).
- Assume that all points in the model are close to each other with respect to the distance to the source. Then the source vector doesn't vary much (and can be assumed to not vary with x---ignoring the possibility that it is ocluded), and the distance doesn't vary much either, and we can roll the constants together to get:

$$\square_d(x)(N(x) \bullet S_d)$$