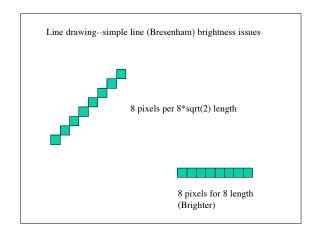
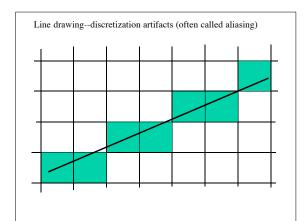
#### Issues

- End points may not be integral due to clipping (or other reasons)
- Brightness is a function of slope.
- Discretization problems "aliasing" (related to previous point).

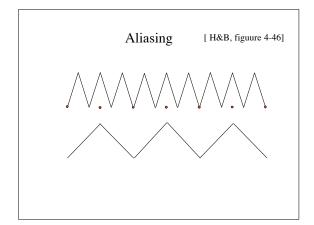


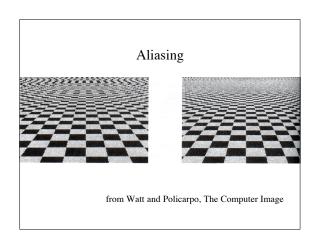


# [ H&B, pp 214-221]

## Aliasing

- We are using discrete binary squares to represent perfect mathematical entities
- To get a value for that that square we used a "sample" at a particular discrete location.
- The sample is somewhat arbitrary due to the choice of discretization, and reflects our discretization (leading to the jagged edges)
- Insufficent samples mean that higher frequency parts of the signal can "alias" (masquerade as) lower frequency information.



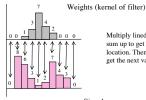


## Aliasing (cont)

- Points and lines as discussed so far have no width so to be visible we concocted a way to sample them based on which discrete cell was closer
- General approach to reducing aliasing is to exploit ability to draw levels of gray between black and white.
- Example--give the line some width; brightness is proportional to area that pixel shares with line
- A more principled approach (which subsumes the above) is to "filter" before sampling.

### Linear Filters (background)

General process: Form new image whose pixels are a weighted sum of original pixel values, using the same set of weights at each point.

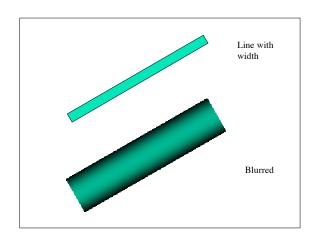


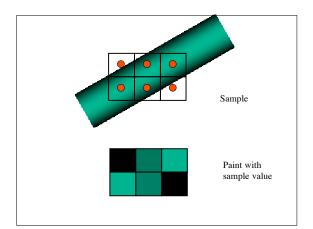
Multiply lined up pairs of numbers and then sum up to get weighted average at the filter location. Then shift the filter and do the same to get the next value.

Signal

### Aliasing via filtering and then sampling

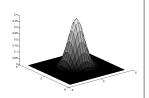
- A filter can be thought of as a weighted average. The weights are given by the filter function. (Examples to come).
- Conceptually, we smooth (convolve) the object to be drawn by applying the filter to the mathematical representation.
- This blurs the object, widens the area it occupies
- Now we "sample" the blurred image--i.e., report the value of the blurred function at the (x,y) of interest, and then fill the square with that brightness.
- (**Technically** we only need to compute the blur at the sampling locations)





# Aliasing via filtering and then sampling

- · Ideal filter is usually Gaussian
- Easier and much faster to approximate Gaussian with a cone

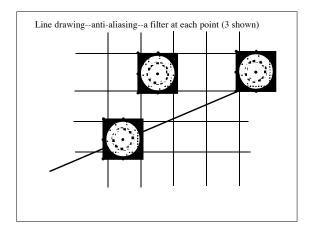


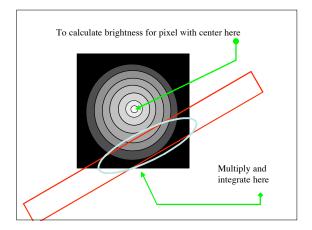
# Anti-aliasing via filtering and then sampling

Technically we "convolve" the function representing the primitive g(x,y) with the filter, h([],[])

$$g \quad h = \iiint g(x \square / y \square / h(/ / ) d / d / d)$$

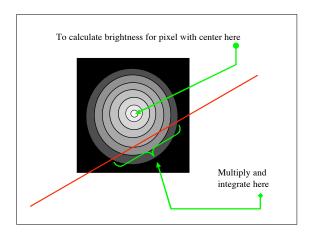
Exact expression is optional

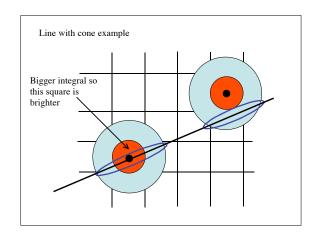




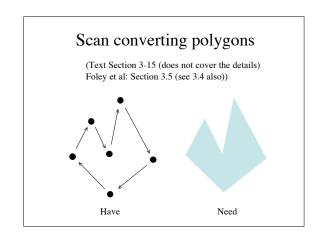
## Line with no width

- If line has no width, then it is a line of "delta" functions.
- Algorithmically simpler: Just integrate intersection of blurring function and line in 1D (along the line).
- Normalization--ensure that if the line goes through the filter center, that the pixel gets the full color of the line.





# Approximating a Gaussian filter with a cone Parabolic boundary which can be approximated with the lines shown in red. In either case, an analytical solution can be computed so that filtering can be done by a formula (rather than numerical integration).

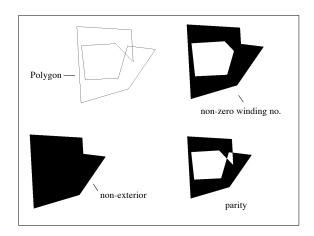


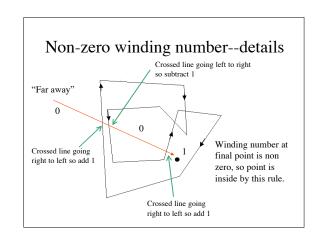
## Filling polygons

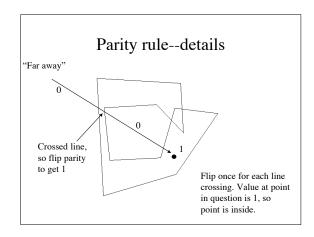
- Polygons are defined by a list of edges each is a pair of vertices (order counts)
- Assume that each vertex is an integer vertex, and polygon lies within frame buffer
- Need to define what is inside and what is outside

## What is inside?

- Easy for simple polygons no self intersections
- For general polygons, three rules are used:
  - non-exterior rule
    - (Can you get arbitrarily far away from the polygon without crossing a line)
  - non-zero winding number rule
  - parity rule (most common--this is the one we will generally used)

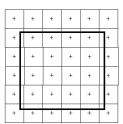






## Which pixel is inside?

- Each pixel is a *sample*, at coordinates (x, y).
  - imagine a piece of paper, where coordinates are continuous
  - pixels are samples on a grid of a drawing on this piece of paper.
- If ideal point (corresponding to grid center) is inside, pixel is inside. (Easy case)



# Which pixel is inside?

In the context of the sweep fill algorithm to come soon: Suppose we are sweeping from left to right. Then for pixels with fractional intersections:

- Going from outside to inside, then take true intersection, and round up to get first interior point.
- Going from inside to outside, then take true intersection, and round down to get last interior point.

Note that if we are considering an adjacent polygon, 1) and 2) are reversed, so it should be clear that for most cases, the pixels owned by each polygon is well defined (and we don't erase any when drawing the other polygon).