ISTA 352
Lecture 24
Light interacting with the world

Administrivia

- I will accept questions for the bonus assignment through the weekend. (We are late getting the video up).

- Homework 3B due Sunday Oct 21
Light interacting with the world

- The light captured by camera carries information about what is in the world because what is in the world interacts with it differently depending on 1) surface properties; and 2) geometry.

- Many effects when light strikes a surface. It could be:
  - absorbed
  - transmitted
  - reflected
  - scattered (in a variety of directions!)

Lambertian surfaces

- Simple special case of reflectance: ideal diffuse or matte surface--e.g. cotton cloth, matte paper.

- Surface appearance is independent of viewing angle.

- Typically such a surface is the result of lots of scattering—the light “forgets” where it came from, and it could end up going in any random direction.

- What counts is how much light power reaches the surface
Lambertian Reflection

Why is brightness proportional to \( n \cdot s \)?

Intuitive argument: The surface scatters light in all directions equally, but as the angle of the light becomes oblique, the amount of light per unit area received is reduced (foreshortened) by a factor of the cosine of the angle.

The sun is far away so light rays are nearly parallel.

The same light spread over \( a \), giving intensity, \( i_a \), is also spread over \( b \), giving intensity, \( i_b \). This means that:

\[
a \cdot i_a = b \cdot i_b
\]

or, because \( a \) is the length of the perpendicular,

\[
i_b = i_a \left( \frac{a}{b} \right) = i_a \cos(\theta)
\]

The sun is far away so light rays are nearly parallel.
Lambertian surfaces

- Surface brightness is only a function of the foreshortening of the incident light (the more oblique it is, the less bright the surface).

- Question: Is the moon a Lambertian reflector?

The moon
Distant light source (sun)

Lambertian reflection
Distant light source

Ideal Mirrors

The opposite extreme case from Lambertian is a mirror.

Instead of going every way equally, the reflected light goes exactly one way.

Reflection Direction

The two angles are equal

The three vectors are coplanar!

\[
\hat{s} + \hat{r} = k\hat{n}
\]

\[
\hat{n} \cdot \hat{s} + \hat{n} \cdot \hat{r} = k \Rightarrow k = 2\hat{n} \cdot \hat{s}
\]

So
\[
\hat{r} = 2(\hat{n} \cdot \hat{s})\hat{n} - \hat{s}
\]
Specularities

Vermeer, Young Woman with a Water Pitcher c. 1664-65;

Rembrandt, Self Portrait 1629; Oil on canvas; The Mauritshuis, The Hague
Specular surfaces

- Important point: The specular part of the reflected light usually carries the color of the light
- Technically, this is the case for dielectrics--plastics, paints, glass.
- Important exception is metals (e.g. gold, copper)
Shadows

Shadows cast by a point source

- A point that can’t see the source is in its shadow
- For point sources, the geometry is simple
- For extended sources, we have an umbra (points seeing no light), and a penumbra (seeing some parts of the light but not all)

The Shadow Identification Problem

Material Edge  Shadow Edge

Shadows in paintings
Shadows in paintings

- Shadows help the 3D illusion a lot, but they need not be mathematically correct or consistent
- The human vision system uses shadows as cues, but does not seem to care much about global consistency
  - Perhaps too hard to compute to evolve?
  - Evolving to be able to verify that the real world is “real” might not make a lot of sense
  - Figuring out why shadows are where they are, or whether they are missing, as an exercise can be hard (try it at home!)

More examples of locally reasonable, globally inconsistent

M.C. Escher, *Waterfall*, 1961
M.C.Esher, *Belvedere*, 1960

M.C.Esher, *Ascending and Descending*, 1960

M.C.Esher, *Print Gallery*, 1956